

See discussions, stats, and author profiles for this publication at: <https://www.researchgate.net/publication/326364769>

Carbon Dioxide and Ocean Acidification

Article in *European Scientific Journal* · June 2018

DOI: 10.19044/esj.2018.v14n18p476

CITATIONS

0

READS

298

1 author:



[P. Stallinga](#)

Universidade do Algarve

94 PUBLICATIONS 2,002 CITATIONS

[SEE PROFILE](#)

Some of the authors of this publication are also working on these related projects:



Macroeconomy [View project](#)



Anthropogenic contributions to climate change [View project](#)

Carbon Dioxide and Ocean Acidification

Peter Stallinga, PhD

University of the Algarve, FCT-DEEI and CEOT, Portugal

Doi: 10.19044/esj.2018.v14n18p476 [URL:http://dx.doi.org/10.19044/esj.2018.v14n18p476](http://dx.doi.org/10.19044/esj.2018.v14n18p476)

Abstract

One of the results of Anthropogenic Global Warming is the acidification of the oceans which threatens wildlife on this planet. In this work it will be shown what will be the effect of carbon dioxide injected into the atmosphere, doubling the total amount from 350 ppm to 700 ppm. Principally the effect on carbonate ions CO_3^{2-} . It is based on textbook chemical principles worked out by numerically solving the resulting non-linear equations by the bisection method. The results are the following: In a pure-water environment the effect is that carbonate ion concentration remains unaltered (i.e., no harm to coral reefs). In a constant-pH environment the carbonate ion concentration grows linearly with CO_2 in the atmosphere (i.e., good for coral reefs). When lowering the pH by other means than CO_2 , the carbonate ion concentration drops linearly (i.e., bad for coral reefs). In some specific cases can raising the CO_2 in the atmosphere slightly reduce carbonate ions in the oceans.

Keywords: Ocean acidification, coral reefs, Le Châtelier

Introduction

A search in the Web of Knowledge results in nearly five thousand hits on "acidification of the oceans". It is a concept that apparently worries the scientific and political communities alike. When the acidity of the oceans increases, so the idea goes, wild life in the oceans will suffer or even die (Silverman, Lazar, Cao, Caldeira, and Erez, 2009). An example is the starving of coral reefs by the depletion of their primary construction material, carbonate ions CO_3^{2-} , used for making their exoskeletons (Hoegh-Guldberg et al., 2007; Kleypas et al., 1999). Newspapers alarmingly report of "bleaching of the coral reefs". As stewards of this planet we have the responsibility to take good care of all life on this planet, including in the seas. As such, we cannot allow entire species to be at risk of extermination because of our human behavior. It has been said that it is our behavior, through the production of carbon dioxide by burning fossil fuels, that causes this increase in acidity of the oceans and the mass death of species within them (Royal Society, 2005).

Knowing that media tend to exaggerate, we can do our own research.

A small study learns that oceans, in fact, are not acidic, but basic. Indeed, the pH of the oceans is about 8.14 (Jacobson, 2005), which is slightly basic. However, the same paper of Jacobson mentions that it has dropped from 8.25 and this is attributed to the increase of CO₂ in the atmosphere that is absorbed by the oceans. Therefore, it might well be that in the future the pH drops below 7 and the oceans turn acidic. In any case, depriving sea life of the necessary ingredient of CO₃²⁻ cannot be beneficial.

Many studies mention the negative effect of CO₂ on sea life. All these studies make a logical error, namely this: CO₂ lowers the pH of the oceans. A lower pH is bad for sea life. Therefore, CO₂ is bad for sea life. As an example, Ware reports that "... it frequently has been thought that coral reefs function as sinks of global atmospheric CO₂. However, the precipitation of calcium carbonate is accompanied by a shift of pH that results in the release of CO₂" (Ware, Smith, and Reaka-Kudla, 1991). Similar conclusions are reached by Michaelis. NOAA summarizes his work as: "Specimens of *Mytilus galloprovincialis* that were maintained for three months at pH = 7.3 (consistent with a pCO₂ of about 1900 µatm) experienced significant reduction in growth, as well as shell dissolution, in response to reduced haemolymph bicarbonate levels". Michaelidis writes in the abstract of his paper "The results obtained in the present study strongly indicate that a reduction in sea-water pH to 7.3 may be fatal for the mussels." (Michaelidis, Ouzounis, Paleras, and Pörtner, 2005). Similarly, the (self acclaimed) authority on Climate Change, the IPCC, writes in its Fourth Assessment Report, "Increasing atmospheric CO₂ concentrations lower oceanic pH and carbonate ion concentrations, thereby decreasing the saturation state with respect to calcium carbonate" (Solomon et al., 2007). Without giving more examples, it is obvious that this is the consensus in literature. For completeness' sake, we also point out here that there are other explanations given for coral bleaching, namely the rise of ocean temperatures. See for instance the work of Hoegh-Guldberg (Hoegh-Guldberg, 1999). (Without going into detail, we are critical of such conclusions, since coral reefs exist in a wide variety of temperatures, and are moreover concentrated in the warmer zones of our planet. Wikipedia: "Although corals exist both in temperate and tropical waters, shallow-water reefs form only in a zone extending from approximately 30° N to 30° S of the equator." Warming of our planet would therefore seem beneficial for coral reefs, which leaves us with the ocean acidification to explain the observed data).

In this work we study the effect of CO₂ on CO₃²⁻ and will show that the effects of increments of atmospheric CO₂ range from no effect (in a clean water environment) to a linear increase of the concentration of CO₃²⁻ in the ocean (in a more realistic constant-pH basic environment). In special cases CO₂ can reduce the amount of CO₃²⁻ in the oceans.

Results and discussion:

All chemical equations are equilibrium equations of the type



the equilibrium constant of which is given by

$$K = \frac{[X]^p [Y]^q}{[A]^m [B]^n}, \quad (2)$$

where the square brackets indicate the concentration of the reactant enclosed in the brackets. The important thing is that, because the equilibrium reaction constant is indeed constant, adding a reactant on one side of the reaction will drive the reaction towards the other side. This is Le Châtelier's principle. As an example, if we increase the concentration of A in the above reaction, [B] will decrease, and [X] and [Y] will increase until the equilibrium ratio as given in Eq. (2) is restored. In no way can adding reactants on one side of the reaction drive the reaction towards that side of the reaction.

The chemistry of carbon dioxide is quite complex, but it boils down to reactions as in Eq. (1). In the first step, CO₂ of the atmosphere dissolves into the ocean



In water the CO₂ molecules combine with water molecules to form H₂CO₃, and this reaction can be written as



Here the ratio of the two concentrations of Eq. (I) is given by Henry's Constant, that depends on the temperature (see Table 6-7 of Lide and Frederikse (1974)),

$$K_h(T) = \frac{[\text{CO}_2(\text{g})]}{[\text{CO}_2(\text{aq})]}. \quad (3)$$

In ice core data we can recognize that the CO₂ gas in the atmosphere lags behind the temperature of the atmosphere by about 700 years (Indermühle, Monnin, Stauffer, Stocker, and Wahlen, 2000). The above ratio also implies that when we inject carbon dioxide into the atmosphere, most of it will wind up in the oceans. It is estimated that about 95% of anthropogenic (or other) carbon dioxide winds up in the oceans and that the residence time of the carbon dioxide in the atmosphere is less than a decade (Essenhigh, 2009; Starr, 1992). Moreover, recent El Niño warming of the oceans caused a serious out-gassing of dissolved carbon dioxide.

Henceforward all reactants are in water, so we omit the designation '(aq)' from now on. In the second step, the dissolved carbon dioxide reacts in an acid-base reaction with water to form bicarbonate ions and protons,



Such reactions are of the general acid-base reaction form of Table 8-43 of Lide and Frederikse (1974),



where HB is a generic acid that dissociates into the B⁻ conjugate base of the acid and a hydrogen ion H⁺ which combines with a water molecule to make a hydronium ion H₃O⁺. The reaction is characterized by the acid dissociation constant, or pK_a value

$$K_a = \frac{[\text{B}^-][\text{H}^+]}{[\text{HB}]} \text{ (mol/L)}, pK_a \equiv -\log_{10} \left(\frac{K_a}{1 \text{ mol/L}} \right), \quad (4)$$

in this case

$$K_{a1} = \frac{[\text{HCO}_3^-][\text{H}^+]}{[\text{H}_2\text{CO}_3]} = 4.47 \times 10^{-7} \text{ mol/L}, pK_a = 6.35. \quad (5)$$

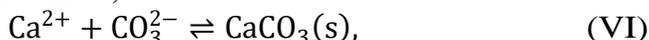
(The value at 25 °C from Table 8-43 of Lide and Frederikse (1974)). This bicarbonate further reacts with water to form carbonate ions and another proton,



with an acid dissociation constant given by [10]

$$K_{a2} = \frac{[\text{CO}_3^{2-}][\text{H}^+]}{[\text{HCO}_3^-]} = 4.68 \times 10^{-11} \text{ mol/L}, pK_a = 10.33. \quad (6)$$

Finally, the carbonate ions react with calcium ions dissolved in water to form solid calcium carbonate,



which is the basic ingredient of seashells and corals.

Indeed, if CO₂ is added to the atmosphere, it will dissolve into the ocean and turn the water acidic (or, to be more precise, less alkaline, since the pH of the oceans is around 8.1). In normal circumstances, Le Châtelier's principle tells us that decreasing the pH (increasing [H⁺]) would drive reaction (V) to the left, thus reducing [CO₃²⁻] and thus pulling reaction (VI) to the left too, reducing the amount of solid calcium carbonate, effectively dissolving an amount of shells and corals in the ocean, including shells and exoskeletons on the sea floor.

However, this is true only when the source of protons is other than CO₂, since CO₂ is exactly what is driving driving reaction (II), and thus reaction (III) and thus reaction (V) to the right and thus what increases the concentration of CO₃²⁻ and the amount of shells. We thus conclude at this point that burning fossil fuels might, in fact, *increase* corals and sea shells in general. In other words, acid rain, when the acid is in the form of sulphuric or nitric acid, dissolves shells, while carbonic-acid rain does not necessarily dissolve them.

Some researchers, for instance NOAA at their home pages (NOAA, 2017), give a calcium-carbonate destroying reaction,

claiming that adding CO_2 to the water will consume carbonate ions, as per the reaction



an acid-base reaction with a single proton hopping from one molecule to the other. The dimensionless reaction constant is given by

$$K_{a3} = \frac{[\text{HCO}_3^-]^2}{[\text{H}_2\text{CO}_3][\text{CO}_3^{2-}]}. \quad (7)$$

Indeed if only CO_2 (that is, H_2CO_3) is added on the left side of reaction (VII), the reaction will be driven to the right and consume CO_3^{2-} . However, as we have seen in reaction (III), adding CO_2 in fact also increases the HCO_3^- concentration and thus, according to Le Châtelier's principle, the reaction might be driven to the left! Adding CO_2 will not deplete CO_3^{2-} , but can even increase it and this will enable growth of corals and shells (if there is enough calcium dissolved in the oceans).

The reaction constant K_{a3} cannot be found in literature, but it can easily be expressed in terms of the other two acid dissociation constants. Combining Eqs. (5) and (6) we find

$$K_{a3} = \frac{K_{a1}}{K_{a2}} = 9.55 \times 10^3. \quad (8)$$

Before we start our calculations, we need to add one more reaction. Water is also an acid-base dissociation reaction, or self-ionization reaction,



with the reaction governed by the constant

$$K_w = [\text{H}^+][\text{OH}^-] = 1.0 \times 10^{-14} (\text{mol/L})^2, \quad (9)$$

implying

$$[\text{OH}^-] = \frac{10^{-14} (\text{mol/L})^2}{[\text{H}^+]}. \quad (10)$$

We have now all ingredients to reason and calculate what will happen when increasing carbon dioxide in the atmosphere. We get one additional condition that the total amount of positive charge must be equal to the total amount of negative charge,

$$[\text{H}^+] = [\text{HCO}_3^-] + 2 \times [\text{CO}_3^{2-}] + [\text{OH}^-]. \quad (11)$$

These equations imply that the effect of doubling CO_2 in the atmosphere on the concentration of CO_3^{2-} in these oceans is minimal. That the effect is minimal is clear once we understand that in the first acid-base reaction, (III), the concentrations of $[\text{HCO}_3^-]$ and $[\text{H}^+]$ are nearly equal (since the second acid-base reaction, (V), does not produce much H^+). Doubling $[\text{H}_2\text{CO}_3]$ will thus mean that $[\text{HCO}_3^-]$ and $[\text{H}^+]$ are multiplied by the square root of 2. In the second acid-

base reaction, (V), they then cancel each other out, and $[CO_3^{2-}]$ remains unaltered, $[CO_3^{2-}] \approx K_{a2}$.

We can even give numerical examples of some specific cases, what will be done now. We start with the observation that it is more common to express the gas-phase CO_2 in terms of partial pressure, see for instance Table 6-7 of Lide and Frederikse (1974). As an example, at 25 °C at 5 kPa partial pressure of CO_2 in the atmosphere (about 5 parts per 100), the equilibrium concentration is 3.1×10^{-6} mole fraction CO_2 in the water. At 350 ppm it is then 2.17×10^{-8} mole fraction. With 55.55 moles H_2O in a liter of water, the CO_2 concentration in water (at 25 degrees) below this 350-ppm atmosphere is

$$\text{at 350 ppm: } [H_2CO_3] = 1.2 \times 10^{-5} \text{ mol/L.} \quad (12)$$

Combining Equations (5), (6), (10), (11) and (12) we find

$$[HCO_3^-] = [H^+] = 2.32 \times 10^{-6} \text{ mol/L (pH = 5.63),}$$

$$\text{at 350 ppm: } [CO_3^{2-}] = 4.67 \times 10^{-11} \text{ mol/L.} \quad (13)$$

(These results were found by solving a third-degree polynomial equation by means of the bisection method (Press, 1989)). If we now double the amount of CO_2 in the atmosphere and repeat the calculations, we get

$$[H_2CO_3] = 2.4 \times 10^{-5} \text{ mol/L,}$$

$$[HCO_3^-] = [H^+] = 3.28 \times 10^{-6} \text{ mol/L (pH = 5.48),}$$

$$\text{at 700 ppm: } [CO_3^{2-}] = 4.68 \times 10^{-11} \text{ mol/L.} \quad (14)$$

Sea life will barely notice what is happening in the atmosphere.

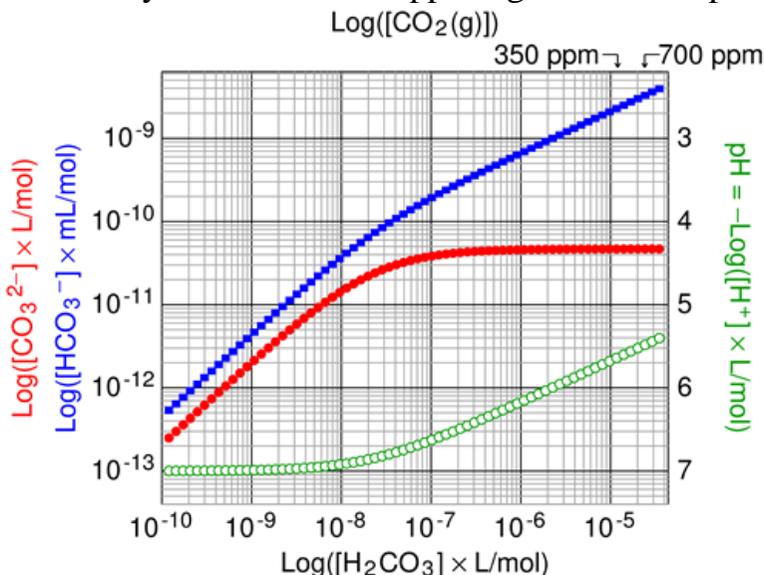
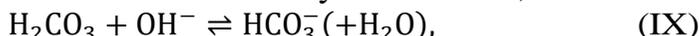


Figure 1: Concentration of carbonate ions (● red full circles) bicarbonate ions (■ blue squares, 1000x scale) and pH (○ green open circles) as a function of concentration of CO_2 in the oceans and air.

Figure 1 gives a summary of the effect that adding CO₂ in the atmosphere has on the pH and concentration of CO₃²⁻ in the oceans when we start with clean water. We see that the bicarbonate ion concentration indeed levels off at [CO₃²⁻]= K₂ = 4.68 x 10⁻¹¹ mol/L.

Let's repeat the calculation for an environment that is closer to the one of the oceans, namely a basic environment with a constant pH, kept constant by some unspecified buffer reaction. While the calculations can be done on basis of H⁺ concentrations using the above equations, they are more elegant when we replace the acid-base reactions given above to the equivalent ones that involve hydroxide-ions,



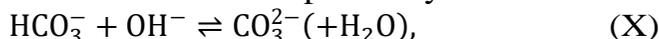
with a reaction constant given by

$$K_{b1} = \frac{[\text{H}_2\text{CO}_3][\text{OH}^-]}{[\text{HCO}_3^-]}. \quad (15)$$

Given the fact that [OH⁻][H⁺] = K_w, this reaction constant is

$$K_{b1} = \frac{K_w}{K_{a1}} = 2.24 \times 10^{-8} \text{ mol/L}. \quad (16)$$

Likewise, the second acid-base reaction is replaced by



with a reaction constant given by

$$K_{b2} = \frac{[\text{HCO}_3^-][\text{OH}^-]}{[\text{CO}_3^{2-}]} = \frac{K_w}{K_{a2}} = 2.14 \times 10^{-4} \text{ mol/L}. \quad (17)$$

If we have a buffered basic environment, both hydronium and hydroxide concentrations ([H⁺] and [OH⁻]) are constant. At this moment the buffer itself is irrelevant; what matters is that some phenomena is keeping the pH constant. Note that the charge neutrality equation (Eq. 11) is maintained by the production or annihilation of the conjugate base.

We can then easily see that any factor in increase in the concentration of carbon dioxide in the atmosphere will cause an equal factor in the increase of [CO₃²⁻] in the oceans. In fact,

$$[\text{CO}_3^{2-}] = \frac{[\text{H}_2\text{CO}_3][\text{OH}^-]^2}{K_{b1}K_{b2}} \quad (18)$$

Taking a typical value of a pH of 8.1 ([OH⁻] = 1.26 × 10⁻⁶ mol/L), we find that for a 350 ppm atmosphere ([H₂CO₃] = 1.2 × 10⁻⁵ mol/L),

$$\begin{aligned} [\text{HCO}_3^-] &= 6.75 \times 10^{-4} \text{ mol/L}, \\ \text{at 350 ppm: } [\text{CO}_3^{2-}] &= 3.98 \times 10^{-6} \text{ mol/L}. \end{aligned} \quad (19)$$

If we now double the amount of CO₂ in the atmosphere and repeat the calculations, we get

$$\begin{aligned} [\text{H}_2\text{CO}_3] &= 2.4 \times 10^{-5} \text{ mol/L}, \\ [\text{HCO}_3^-] &= 1.35 \times 10^{-3} \text{ mol/L}, \end{aligned}$$

at 700 ppm: $[CO_3^{2-}] = 7.96 \times 10^{-6} \text{ mol/L}$. (20)

Figure 2 gives a summary of this constant-pH system. Sea life is very happy with the extra carbon dioxide in the atmosphere! $[CO_3^{2-}]$ grows linearly with $[CO_2]$.

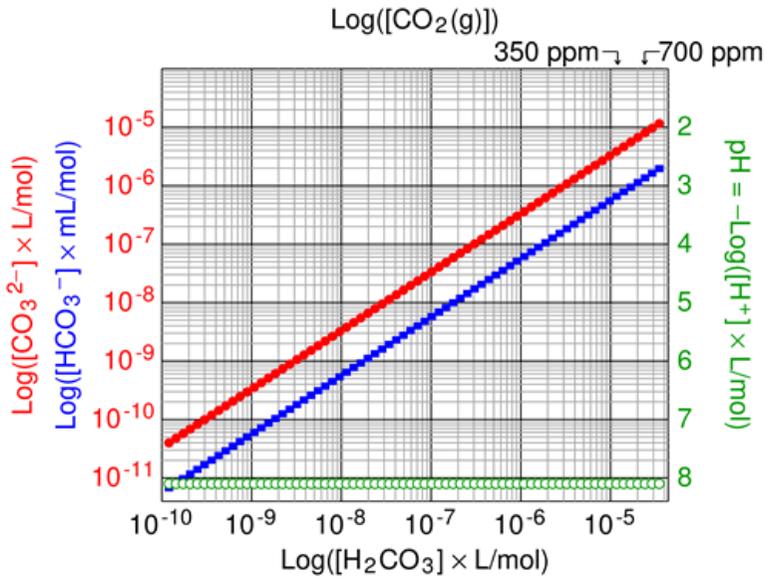


Figure 2: Concentration of carbonate ions (● red full circles) bicarbonate ions (■ blue squares, 1000x scale) and pH (○ green open circles) as a function of concentration of CO₂ in the oceans and atmosphere for a buffered solution with constant pH.

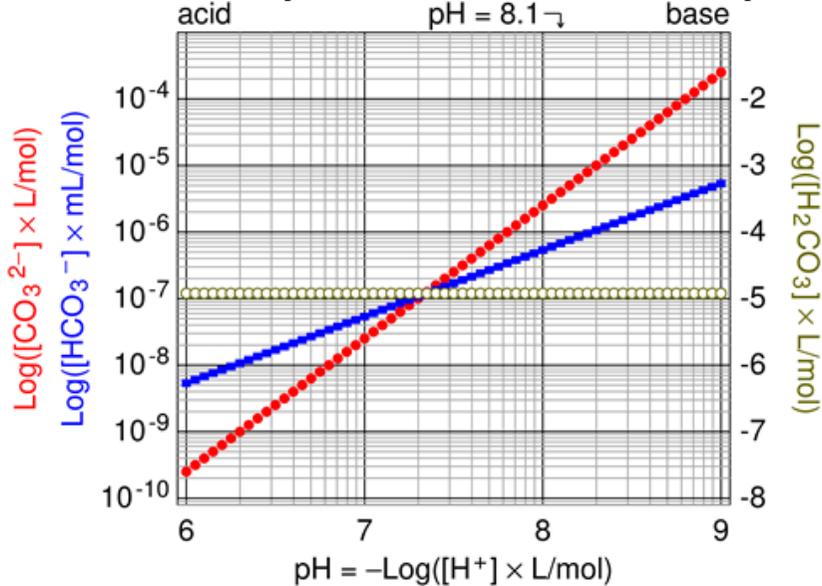
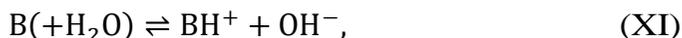


Figure 3: Concentration (as a function of pH) of carbonate ions (● red full circles) bicarbonate ions (■ blue squares, 1000x scale) and H₂CO₃ (○ brown open circles) in the oceans below an atmosphere with (constant) 350 ppm concentration CO₂.

Now let's repeat the above calculation for systems where not the carbon dioxide concentrations (in air and sea) change, but some other reaction produces hydrogen ions thereby changing the pH of the oceans (for instance raining sulphuric acid, creating H^+ , HSO_4^- and SO_4^{2-}) while the concentration of carbon dioxide above and in them remains the same. As can easily be shown, the end result is the same equation, Eq. 18. Figure 3 summarizes the effect of varying the pH (by other means than carbonic acid). Acids kill coral reefs.

It has to be noted that for these last calculations, the concentration of CO_2 in the atmosphere (and H_2CO_3 in the oceans) is assumed to be constant. In many approaches the (chemistry) researchers make the logical error of assuming a constant carbon mass (following Lavoisier's principle) as often occurs in laboratory experiments, which are closed systems (for example test tubes). In this latter case the carbonate ion concentration can rise as well as fall for varying pH. In the current analysis, the concentration in the atmosphere is a given fact (a parameter) and the rest results from simple chemistry equations as shown above.

Finally, we will show how for some specific cases of semi-depleted buffers, the concentration of carbonate ions can decrease upon adding carbon dioxide in the oceans. To show this we have to simulate a real buffer with non-infinite resistance to pH changes. The first step is to create a buffer solution. We do this by adding a weak base molecule B to water (for instance NH_3), that is a source of hydroxide ions by capturing a proton from water:



with a reaction constant given by

$$K_{\text{buffer}} = \frac{[BH^+][OH^-]}{[B]}. \quad (21)$$

We set this to $K_{\text{buffer}} = 10^{-5.9}$ mol/L so that the target pH will be 8.1, as will be shown. In this solution (C mol/L) we add an equal amount of salt BHS (for instance NH_4Cl) that is another source of conjugate acid ions,



We assume the reaction constant so large that effectively all salt is dissociated into ions and the negative ion concentration is equal to the original concentration of BHS added to the solution, $[S^-] = C$. We thus have a total concentration of conjugated base molecule in solution equal to

$$[BH^+] = 2C - [B] \quad (22)$$

one contribution (C) comes from the dissolved salt and the second contribution ($C-[B]$) from the base that was protonated. Our charge-neutrality condition now becomes

$$[H^+] + [BH^+] = [HCO_3^-] + 2 \times [CO_3^{2-}] + [OH^-] + [S^-]. \quad (23)$$

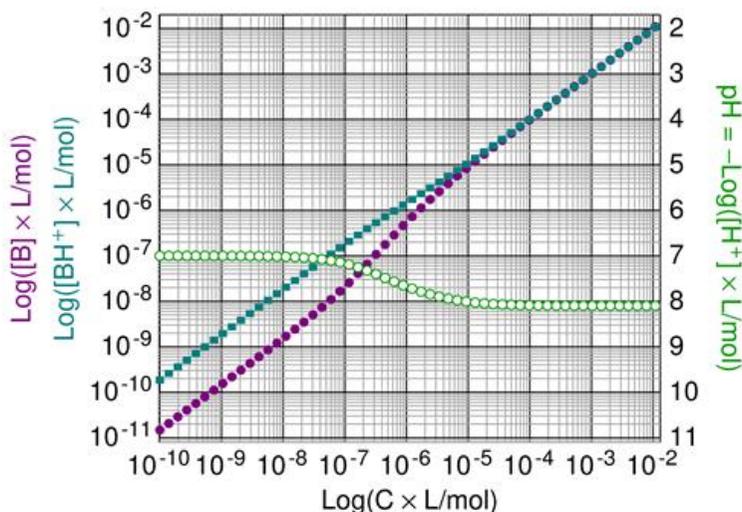


Figure 4: Concentration of base molecules (● purple full circles) conjugated-acid ions (■ cyan squares) and pH (○ green open circles) as a function of C equal to $[S^-]$ in a buffer solution without CO_2 .

This was combined with the CO_2 -related equations (Eqs. 15-17) and solved for various situations by the zero-finding bisection method described earlier. The first situation is one without any carbon, only varying the concentration of buffer ingredients (C). This is shown in Figure 4. We see that for increasing C the pH settles at the target value 8.1, there where the concentrations of base and conjugated acid become equal, $[B] = [BH^+] = C$. This figure is a confirmation of the Henderson-Hasselbalch equation, $pH = 14 - pK_{buffer} + \text{Log}([B]/[BH^+])$.

The next step is to vary the H_2CO_3 concentration in the ocean for various buffer solutions.

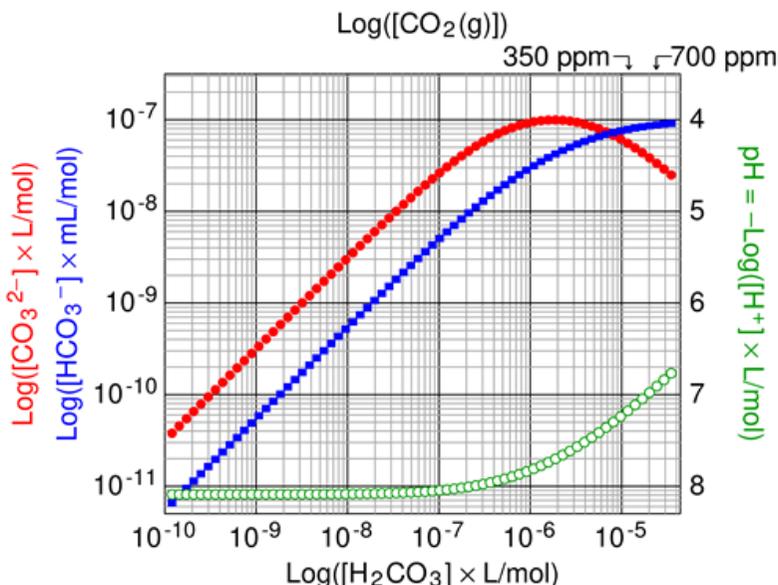


Figure 5: Concentration of carbonate ions (● red full circles) bicarbonate ions (■ blue squares, 1000x scale) and pH (○ green open circles) as a function of concentration of CO₂ in the oceans and atmosphere for a depleted buffer solution with $C = [S] = 10^{-4}$ mol/L.

For large values of C , for instance $C = 1$ mol/L, the constant-pH figure is reproduced (Figure 2). For small concentrations, for instance $C = 10^{-8}$ mol/L, the pure-water figure is reproduced (Figure 1). However, for intermediate values of C , the behavior is (at first sight) peculiar in that for increasing carbon dioxide dissolved in the ocean, $[HCO_3^-]$ rises in the ocean, following the principle of Le Châtelier, but $[CO_3^{2-}]$ is dropping. See for instance Figure 5 for the case of $C = 10^{-4}$ mol/L.

Conclusions:

In conclusion, we have shown here how increasing carbon dioxide in the atmosphere can indeed decrease the pH of the ocean – in principle even turn it acid – but in most cases adds the principal building ingredient of sea shells and coral reefs, carbonate ions. The effects range from completely zero (in the case of a pure ocean) to a linear increase in carbonate-ion density (in case of a buffered, constant pH, environment). In intermediate-buffer cases some carbonate ions can be removed from the ocean by adding carbon dioxide. It shows how we should take care not to take rapid conclusions in thinking that any pH decrease will always destroy food for sea life. Things are a little more complicated than that.

Disclosure of interests:

The author declares not to have any conflict of interests. This research

was paid by no grant. It received no funding whatsoever, apart from his salary at the university where he works. Nor is he member of any climate committees (political or other) or is he linked to companies or NGOs, financially or otherwise. He is not member of any political party or movement. This is an independent work that does not necessarily represent the opinion of his university or of his government. He wishes to thank Prof. Khmelinskii (UAlg) for valuable discussions.

References:

1. Essenhig, R. H. (2009). Potential dependence of global warming on the residence time (rt) in the atmosphere of anthropogenically sourced carbon dioxide. *Energy & Fuels*, 23, 2773–2784. doi:10.1021/ef800581r
2. Hoegh-Guldberg, O. (1999). Climate change, coral bleaching and the future of the world's coral reefs. *Marine Freshwater Research*, 50, 839–866. doi:10.1071/MF99078
3. Hoegh-Guldberg, O., Mumby, P. J., Hooten, A. J., Steneck, R. S., Greenfield, P., Gomez, E., . . . Hatziolos, M. E. (2007). Coral reefs under rapid climate change and ocean acidification. *Science*, 318, 1737. doi:10.1126/science.1152509
4. Indermühle, A., Monnin, E., Stauffer, B., Stocker, T. F., & Wahlen, M. (2000). Atmospheric CO₂ concentration from 60 to 20 kyr bp from the Taylor Dome ice core, Antarctica. *Geophysical Research Letters*, 27, 735–738.
5. Jacobson, M. Z. (2005). Studying ocean acidification with conservative, stable numerical schemes for nonequilibrium air-ocean exchange and ocean equilibrium chemistry. *Journal of Geophysical Research*, 110, D07302. doi:10.1029/2004JD005220
6. Kleypas, J. A., Buddemeier, R. W., Archer, D., Gattuso, J.-P., Langdon, C., & Opdyke, B. N. (1999). Geochemical consequences of increased atmospheric carbon dioxide on coral reefs. *Science*, 284, 118–120. doi:10.1126/science.284.5411.118
7. Lide, D. R. & Frederikse, H. P. R. (Eds.). (1974). CRC handbook of chemistry and physics 77th edition. CRC Press.
8. Michaelidis, B., Ouzounis, C., Paleras, A., & Pörtner, H. O. (2005). Effects of long-term moderate hypercapnia on acid-base balance and growth rate in marine mussels *Mytilus galloprovincialis*. *Marine Ecology Progress Series*, 293, 109–118.

9. NOAA (2017). Ocean acidification. Retrieved November 10, 2017, from <http://www.noaa.gov/resource-collections/ocean-acidification>
10. Press, W. H., Teukolsky, S. A., Vetterling, W. T., & Flannery, B. P. (1989). *Numerical recipes in pascal (first edition): the art of scientific computing*. Cambridge University Press.
11. Royal Society (2005). *Ocean acidification due to increasing atmospheric carbon dioxide*. Clyvedon Press, Cardiff, U. K.
12. Silverman, J., Lazar, B., Cao, L., Caldeira, K., & Erez, J. (2009). Coral reefs may start dissolving when atmospheric CO₂ doubles. *Geophysical Research Letters*, 36, L05606. doi:10.1029/2008GL036282
13. Solomon, S., Qin, D., Manning, M., Chen, Z., Marquis, M., Averyt, K. B., . . . Miller, H. L. (Eds.). (2007). *IPCC, 2007: climate change 2007: the physical science basis. contribution of working group I to the fourth assessment report of the intergovernmental panel on climate change*. Cambridge University Press.
14. Starr, C. (1992). Atmospheric CO₂ residence time and the carbon cycle. *Energy*, 18, 1297–1310. doi:10.1016/0360-5442(93)90017-8
15. Ware, J. R., Smith, S. V., & Reaka-Kudla, M. L. (1991). Coral reefs: